

# DESIGN OF MACHINERY

AN INTRODUCTION TO THE SYNTHESIS AND  
ANALYSIS OF MECHANISMS  
AND MACHINES

Second Edition

TÀI LIỆU LƯU HÀNH NỘI BỘ  
KHÔNG MUA BÁN, SAO CHÉP



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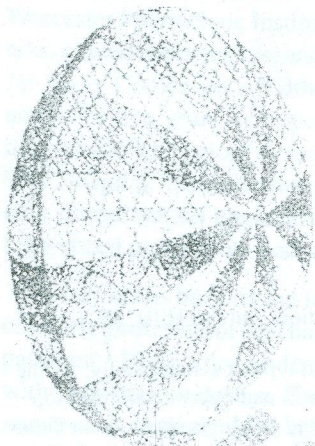
# DESIGN OF MACHINERY

## AN INTRODUCTION TO THE SYNTHESIS AND ANALYSIS OF MECHANISMS AND MACHINES

Second Edition

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# CONTENTS

Preface to the Second Edition .....	XVII
Preface to the First Edition .....	XIX

## PART I KINEMATICS OF MECHANISMS ..... 1

### Chapter 1 Introduction ..... 3

1.0 Purpose .....	3
1.1 Kinematics and Kinetics .....	3
1.2 Mechanisms and Machines .....	4
1.3 A Brief History of Kinematics .....	5
1.4 Applications of Kinematics .....	6
1.5 The Design Process .....	7
<i>Design, Invention, Creativity</i> .....	7
<i>Identification of Need</i> .....	8
<i>Background Research</i> .....	9
<i>Goal Statement</i> .....	9
<i>Performance Specifications</i> .....	9
<i>Ideation and Invention</i> .....	10
<i>Analysis</i> .....	11
<i>Selection</i> .....	12
<i>Detailed Design</i> .....	13
<i>Prototyping and Testing</i> .....	13
<i>Production</i> .....	13
1.6 Other Approaches to Design .....	14
<i>Axiomatic Design</i> .....	15
1.7 Multiple Solutions .....	15
1.8 Human Factors Engineering .....	15
1.9 The Engineering Report .....	16
1.10 Units .....	16
1.11 What's to Come .....	16
1.12 References .....	18
1.13 Bibliography .....	19
	20

### Chapter 2 Kinematics Fundamentals ..... 22

2.0 Introduction .....	22
2.1 Degrees of Freedom .....	22
2.2 Types of Motion .....	22
2.3 Links, Joints, and Kinematic Chains .....	23
2.4 Determining Degree of Freedom .....	24
<i>Degree of Freedom in Planar Mechanisms</i> .....	28
<i>Degree of Freedom in Spatial Mechanisms</i> .....	29
.....	32
2.5 Mechanisms and Structures .....	32
2.6 Number Synthesis .....	33
2.7 Paradoxes .....	33
2.8 Isomers .....	37
2.9 Linkage Transformation .....	38
2.10 Intermittent Motion .....	40
2.11 Inversion .....	42
	44

2.12	The Grashof Condition .....	4
	<i>Classification of the Fourbar Linkage</i> .....	49
2.13	Linkages of More Than Four Bars .....	5
	<i>Geared Fivebar Linkages</i> .....	52
	<i>Sixbar Linkages</i> .....	53
	<i>Grashof-type Rotatability Criteria for Higher-order Linkages</i> .....	53
2.14	Springs as Links .....	5
2.15	Practical Considerations .....	5
	<i>Pin Joints versus Sliders and Half Joints</i> .....	55
	<i>Cantilever versus Straddle Mount</i> .....	57
	<i>Short Links</i> .....	58
	<i>Bearing Ratio</i> .....	58
	<i>Linkages versus Cams</i> .....	59
2.16	Motor and Drives .....	6
	<i>Electric Motors</i> .....	60
	<i>Air and Hydraulic Motors</i> .....	65
	<i>Air and Hydraulic Cylinders</i> .....	65
	<i>Solenoids</i> .....	66
2.17	References .....	6
2.18	Problems .....	6
<b>Chapter 3 Graphical Linkage Synthesis .....</b>		<b>7</b>
3.0	Introduction .....	7
3.1	Synthesis .....	7
3.2	Function, Path, and Motion Generation .....	7
3.3	Limiting Conditions .....	8
3.4	Dimensional Synthesis .....	8
	<i>Two-Position Synthesis</i> .....	83
	<i>Three-Position Synthesis with Specified Moving Pivots</i> .....	89
	<i>Three-Position Synthesis with Alternate Moving Pivots</i> .....	90
	<i>Three-Position Synthesis with Specified Fixed Pivots</i> .....	93
	<i>Position Synthesis for More Than Three Positions</i> .....	97
3.5	Quick-Return Mechanisms .....	9
	<i>Fourbar Quick-Return</i> .....	98
	<i>Sixbar Quick-Return</i> .....	100
3.6	Coupler Curves .....	10
3.7	Cognates .....	11
	<i>Parallel Motion</i> .....	117
	<i>Geared Fivebar Cognates of the Fourbar</i> .....	119
3.8	Straight-Line Mechanisms .....	12
	<i>Designing Optimum Straight-Line Fourbar Linkages</i> .....	122
3.9	Dwell Mechanisms .....	12
	<i>Single-Dwell Linkages</i> .....	126
	<i>Double-Dwell Linkages</i> .....	128
3.10	References .....	13
3.11	Bibliography .....	13
3.12	Problems .....	13
3.13	Projects .....	14
<b>Chapter 4 Position Analysis .....</b>		<b>14</b>
4.0	Introduction .....	14
4.1	Coordinate Systems .....	14
4.2	Position and Displacement .....	14
	<i>Position</i> .....	147
	<i>Displacement</i> .....	147

4.3	Translation, Rotation, and Complex Motion .....	149
	<i>Translation</i> .....	149
	<i>Rotation</i> .....	149
	<i>Complex Motion</i> .....	149
	<i>Theorems</i> .....	150
4.4	Graphical Position Analysis of Linkages .....	151
4.5	Algebraic Position Analysis of Linkages .....	152
	<i>Vector Loop Representation of Linkages</i> .....	153
	<i>Complex Numbers as Vectors</i> .....	154
	<i>The Vector Loop Equation for a Fourbar Linkage</i> .....	156
4.6	The Fourbar Slider-Crank Position Solution .....	159
4.7	An Inverted Slider-Crank Position Solution .....	161
4.8	Linkages of More Than Four Bars .....	164
	<i>The Geared Fivebar Linkage</i> .....	164
	<i>Sixbar Linkages</i> .....	167
4.9	Position of Any Point on a Linkage .....	168
4.10	Transmission Angles .....	169
	<i>Extreme Values of the Transmission Angle</i> .....	169
4.11	Toggle Positions .....	171
4.12	Circuits and Branches in Linkages .....	173
4.13	Newton-Raphson Solution Method .....	174
	<i>One-Dimensional Root-Finding (Newton's Method)</i> .....	174
	<i>Multidimensional Root-Finding (Newton-Raphson Method)</i> .....	176
	<i>Newton-Raphson Solution for the Fourbar Linkage</i> .....	177
	<i>Equation Solvers</i> .....	178
4.14	References .....	178
4.15	Problems .....	178
<b>Chapter 5 Analytical Linkage Synthesis .....</b>		<b>188</b>
5.0	Introduction .....	188
5.1	Types of Kinematic Synthesis .....	188
5.2	Precision Points .....	189
5.3	Two-Position Motion Generation by Analytical Synthesis .....	189
5.4	Comparison of Analytical and Graphical Two-Position Synthesis .....	196
5.5	Simultaneous Equation Solution .....	199
5.6	Three-Position Motion Generation by Analytical Synthesis .....	201
5.7	Comparison of Analytical and Graphical Three-Position Synthesis .....	206
5.8	Synthesis for a Specified Fixed Pivot Location .....	211
5.9	Center-Point and Circle-Point Circles .....	217
5.10	Four- and Five-Position Analytical Synthesis .....	219
5.11	Analytical Synthesis of a Path Generator with Prescribed Timing .....	220
5.12	Analytical Synthesis of a Fourbar Function Generator .....	220
5.13	Other Linkage Synthesis Methods .....	224
	<i>Precision Point Methods</i> .....	226
	<i>Coupler Curve Equation Methods</i> .....	227
	<i>Optimization Methods</i> .....	227
5.14	References .....	230
5.15	Problems .....	232
<b>Chapter 6 Velocity Analysis .....</b>		<b>241</b>
6.0	Introduction .....	241
6.1	Definition of Velocity .....	241
6.2	Graphical Velocity Analysis .....	244

6.3	Instant Centers of Velocity .....	249
6.4	Velocity Analysis with Instant Centers .....	256
	<i>Angular Velocity Ratio</i> .....	257
	<i>Mechanical Advantage</i> .....	259
	<i>Using Instant Centers in Linkage Design</i> .....	261
6.5	Centrodes .....	263
	A "Linkless" Linkage .....	266
	<i>Cusps</i> .....	267
6.6	Velocity of Slip .....	267
6.7	Analytical Solutions for Velocity Analysis .....	271
	<i>The Fourbar Pin-Jointed Linkage</i> .....	271
	<i>The Fourbar Slider-Crank</i> .....	274
	<i>The Fourbar Inverted Slider-Crank</i> .....	276
6.8	Velocity Analysis of the Geared Fivebar Linkage .....	278
6.9	Velocity of Any Point on a Linkage .....	279
6.10	References .....	280
6.11	Problems .....	281
<b>Chapter 7 Acceleration Analysis .....</b>		<b>300</b>
7.0	Introduction .....	300
7.1	Definition of Acceleration .....	300
7.2	Graphical Acceleration Analysis .....	303
7.3	Analytical Solutions for Acceleration Analysis .....	308
	<i>The Fourbar Pin-Jointed Linkage</i> .....	308
	<i>The Fourbar Slider-Crank</i> .....	311
	<i>Coriolis Acceleration</i> .....	313
	<i>The Fourbar Inverted Slider-Crank</i> .....	315
7.4	Acceleration Analysis of the Geared Fivebar Linkage .....	319
7.5	Acceleration of any Point on a Linkage .....	320
7.6	Human Tolerance of Acceleration .....	322
7.7	Jerk .....	324
7.8	Linkages of <i>N</i> Bars .....	327
7.9	References .....	327
7.10	Problems .....	327
<b>Chapter 8 Cam Design .....</b>		<b>345</b>
8.0	Introduction .....	345
8.1	Cam Terminology .....	346
	<i>Type of Follower Motion</i> .....	347
	<i>Type of Joint Closure</i> .....	348
	<i>Type of Follower</i> .....	348
	<i>Type of Cam</i> .....	348
	<i>Type of Motion Constraints</i> .....	351
	<i>Type of Motion Program</i> .....	351
8.2	<i>S V A J</i> Diagrams .....	352
8.3	Double-Dwell Cam Design—Choosing <i>S V A J</i> Functions .....	353
	<i>The Fundamental Law of Cam Design</i> .....	356
	<i>Simple Harmonic Motion (SHM)</i> .....	357
	<i>Cycloidal Displacement</i> .....	359
	<i>Combined Functions</i> .....	362
8.4	Single-Dwell Cam Design—Choosing <i>S V A J</i> Functions .....	374
8.5	Polynomial Functions .....	378
	<i>Double-Dwell Applications of Polynomials</i> .....	378
	<i>Single-Dwell Applications of Polynomials</i> .....	382

8.6	Critical Path Motion (CPM) .....	385
	<i>Polynomials Used for Critical Path Motion</i> .....	386
	<i>Half-Period Harmonic Family Functions</i> .....	393
8.7	Sizing the Cam—Pressure Angle and Radius of Curvature .....	396
	<i>Pressure Angle—Roller Followers</i> .....	397
	<i>Choosing a Prime Circle Radius</i> .....	400
	<i>Overturning Moment—Flat-Faced Follower</i> .....	402
	<i>Radius of Curvature—Roller Follower</i> .....	403
	<i>Radius of Curvature—Flat-Faced Follower</i> .....	407
8.8	Cam Manufacturing Considerations .....	412
	<i>Geometric Generation</i> .....	413
	<i>Manual or NC Machining to Cam Coordinates (Plunge-Cutting)</i> .....	413
	<i>Continuous Numerical Control with Linear Interpolation</i> .....	414
	<i>Continuous Numerical Control with Circular Interpolation</i> .....	416
	<i>Analog Duplication</i> .....	416
	<i>Actual Cam Performance Compared to Theoretical Performance</i> .....	418
8.9	Practical Design Considerations .....	421
	<i>Translating or Oscillating Follower?</i> .....	421
	<i>Force- or Form-Closed?</i> .....	422
	<i>Radial or Axial Cam?</i> .....	422
	<i>Roller or Flat-Faced Follower?</i> .....	423
	<i>To Dwell or Not to Dwell?</i> .....	423
	<i>To Grind or Not to Grind?</i> .....	424
	<i>To Lubricate or Not to Lubricate?</i> .....	424
8.10	References .....	424
8.11	Problems .....	425
8.12	Projects .....	429
<b>Chapter 9 Gear Trains .....</b>		<b>432</b>
9.0	Introduction .....	432
9.1	Rolling Cylinders .....	433
9.2	The Fundamental Law of Gearing .....	434
	<i>The Involute Tooth Form</i> .....	435
	<i>Pressure Angle</i> .....	437
	<i>Changing Center Distance</i> .....	438
	<i>Backlash</i> .....	438
9.3	Gear Tooth Nomenclature .....	440
9.4	Interference and Undercutting .....	442
	<i>Unequal-Addendum Tooth Forms</i> .....	444
9.5	Contact Ratio .....	444
9.6	Gear Types .....	447
	<i>Spur, Helical, and Herringbone Gears</i> .....	447
	<i>Worms and Worm Gears</i> .....	448
	<i>Rack and Pinion</i> .....	448
	<i>Bevel and Hypoid Gears</i> .....	449
	<i>Noncircular Gears</i> .....	450
	<i>Belt and Chain Drives</i> .....	450
9.7	Simple Gear Trains .....	452
9.8	Compound Gear Trains .....	453
	<i>Design of Compound Trains</i> .....	454
	<i>Design of Reverted Compound Trains</i> .....	456
	<i>An Algorithm for the Design of Compound Gear Trains</i> .....	458
9.9	Epicyclic or Planetary Gear Trains .....	462
	<i>The Tabular Method</i> .....	464
	<i>The Formula Method</i> .....	469
9.10	Efficiency of Gear Trains .....	470

9.11	Transmissions .....	474
9.12	Differentials .....	477
9.13	References .....	479
9.14	Problems .....	479
<b>PART II DYNAMICS OF MACHINERY .....</b>		<b>489</b>
<b>Chapter 10 Dynamics Fundamentals .....</b>		<b>491</b>
10.0	Introduction .....	491
10.1	Newton's Laws of Motion .....	492
10.2	Dynamic Models .....	492
10.3	Mass .....	493
10.4	Mass Moment and Center of Gravity .....	495
10.5	Mass Moment of Inertia (Second Moment of Mass) .....	497
10.6	Parallel Axis Theorem (Transfer Theorem) .....	498
10.7	Radius of Gyration .....	498
10.8	Center of Percussion .....	500
10.9	Lumped Parameter Dynamic Models .....	500
	<i>Spring Constant</i> .....	501
	<i>Damping</i> .....	503
10.10	Equivalent Systems .....	504
	<i>Combining Dampers</i> .....	505
	<i>Combining Springs</i> .....	506
	<i>Combining Masses</i> .....	506
	<i>Lever and Gear Ratios</i> .....	512
10.11	Solution Methods .....	513
10.12	The Principle of d'Alembert .....	515
10.13	Energy Methods—Virtual Work .....	517
10.14	References .....	518
10.15	Problems .....	518
<b>Chapter 11 Dynamic Force Analysis .....</b>		<b>521</b>
11.0	Introduction .....	521
11.1	Newtonian Solution Method .....	522
11.2	Single Link in Pure Rotation .....	525
11.3	Force Analysis of a Threebar Crank-Slide Linkage .....	531
11.4	Force Analysis of a Fourbar Linkage .....	538
11.5	Force Analysis of a Fourbar Slider-Crank Linkage .....	541
11.6	Force Analysis of the Inverted Slider-Crank .....	543
11.7	Force Analysis—Linkages with More Than Four Bars .....	544
11.8	Shaking Forces and Shaking Torque .....	545
11.9	Program FOURBAR .....	545
11.10	Linkage Force Analysis by Energy Methods .....	548
11.11	Controlling Input Torque—Flywheels .....	554
11.12	A Linkage Force Transmission Index .....	556
11.13	Practical Considerations .....	557
11.14	References .....	557
11.15	Problems .....	567
11.16	Projects .....	567



<b>Chapter 12</b>	<b>Balancing</b> .....	<b>570</b>
12.0	Introduction .....	570
12.1	Static Balance .....	571
12.2	Dynamic Balance .....	574
12.3	Balancing Linkages .....	579
	<i>Complete Force Balance of Linkages</i> .....	580
12.4	Effect of Balancing on Shaking and Pin Forces .....	583
12.5	Effect of Balancing on Input Torque .....	585
12.6	Balancing the Shaking Moment in Linkages .....	586
12.7	Measuring and Correcting Imbalance .....	590
12.8	References .....	591
12.9	Problems .....	592
<b>Chapter 13</b>	<b>Engine Dynamics</b> .....	<b>598</b>
13.0	Introduction .....	598
13.1	Engine Design .....	600
13.2	Slider-Crank Kinematics .....	605
13.3	Gas Force and Gas Torque .....	610
13.4	Equivalent Masses .....	614
13.5	Inertia and Shaking Forces .....	617
13.6	Inertia and Shaking Torques .....	620
13.7	Total Engine Torque .....	622
13.8	Flywheels .....	622
13.9	Pin Forces in the Single-Cylinder Engine .....	623
13.10	Balancing the Single-Cylinder Engine .....	631
13.11	Design Trade-offs and Ratios .....	634
	<i>Conrod/Crank Ratio</i> .....	634
	<i>Bore/Stroke Ratio</i> .....	634
	<i>Materials</i> .....	635
13.12	Bibliography .....	635
13.13	Problems .....	635
13.14	Projects .....	638
<b>Chapter 14</b>	<b>Multicylinder Engines</b> .....	<b>639</b>
14.0	Introduction .....	639
14.1	Multicylinder Engine Designs .....	641
14.2	The Crank Phase Diagram .....	644
14.3	Shaking Forces in Inline Engines .....	646
14.4	Inertia Torque in Inline Engines .....	649
14.5	Shaking Moment in Inline Engines .....	650
14.6	Even Firing .....	652
	<i>Two-Stroke Cycle Engine</i> .....	653
	<i>Four-Stroke Cycle Engine</i> .....	655
14.7	Vee Engine Configurations .....	661
14.8	Opposed Engine Configurations .....	674
14.9	Balancing Multicylinder Engines .....	675
	<i>Secondary Balance in the Four-Cylinder Inline Engine</i> .....	679
14.10	References .....	682
14.11	Bibliography .....	682
14.12	Problems .....	682
14.13	Projects .....	683

<b>Chapter 15 Cam Dynamics .....</b>	<b>685</b>
15.0 Introduction .....	685
15.1 Dynamic Force Analysis of the Force-Closed Cam Follower .....	686
<i>Undamped Response</i> .....	686
<i>Damped Response</i> .....	689
15.2 Resonance .....	696
15.3 Kinetostatic Force Analysis of the Force-Closed Cam-Follower .....	698
15.4 Kinetostatic Force Analysis of the Form-Closed Cam-Follower .....	702
15.5 Camshaft Torque .....	706
15.6 Measuring Dynamic Forces and Accelerations .....	709
15.7 Practical Considerations .....	713
15.8 References .....	713
15.9 Bibliography .....	713
15.10 Problems .....	714
 <b>Chapter 16 Engineering Design .....</b>	 <b>717</b>
16.0 Introduction .....	717
16.1 A Design Case Study .....	718
16.2 Closure .....	723
16.3 References .....	723
 <b>Appendix A Computer Programs .....</b>	 <b>725</b>
A.0 Introduction .....	725
A.1 General Information .....	727
A.2 General Program Operation .....	727
A.3 Program FOURBAR .....	735
A.4 Program FIVEBAR .....	743
A.5 Program SIXBAR .....	745
A.6 Program SLIDER .....	749
A.7 Program DYNACAM .....	751
A.8 Program ENGINE .....	757
A.9 Program MATRIX .....	764
 <b>Appendix B Material Properties .....</b>	 <b>765</b>
 <b>Appendix C Geometric Properties .....</b>	 <b>769</b>
 <b>Appendix D Spring Data .....</b>	 <b>771</b>
 <b>Appendix E Atlas of Geared Fivebar Linkage Coupler Curves .....</b>	 <b>775</b>
 <b>Appendix F Answers to Selected Problems .....</b>	 <b>781</b>
 <b>Index .....</b>	 <b>795</b>
 <b>CD-ROM Index .....</b>	 <b>809</b>

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***Thông tin tài trợ!***



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